

## □ 1 Cartesian definitions

```

(%i1) kill(all); numer: false;
(%o0) done
(%o1) false

(%i2) curl(a) := [diff(a[3],y) - diff(a[2],z),
                  diff(a[1],z) - diff(a[3],x),
                  diff(a[2],x) - diff(a[1],y)];
(%o2) curl(a):=[diff(a3,y)-diff(a2,z),diff(a1,z)-diff(a3,x),
diff(a2,x)-diff(a1,y)]

(%i3) div(a) := diff(a[1], x) + diff(a[2], y) + diff(a[3], z);
(%o3) div(a):=diff(a1,x)+diff(a2,y)+diff(a3,z)

```

## □ 2 Rodriguez-Vaz solution

### □ 2.1 Define W and parameters

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(%i4) W: -C*[alpha*Omega*y/r^3 - %beta*x*z/r^5,
           alpha*Omega*x/r^3+%beta*y*z/r^5,
           %beta*(x^2+y^2)/r^5 - 2*alpha/r^3];
(%o4) 
$$\left[ -\left( \frac{\alpha \Omega y}{r^3} - \frac{\beta x z}{r^5} \right) C, -\left( \frac{\beta y z}{r^5} + \frac{\alpha \Omega x}{r^3} \right) C, -\left( \frac{\beta (y^2 + x^2)}{r^5} - \frac{2 \alpha}{r^3} \right) C \right]$$


(%i5) factor(W);
(%o5) 
$$\left[ \frac{(\beta x z - \alpha \Omega r^2 y) C}{r^5}, -\frac{(\beta y z + \alpha \Omega r^2 x) C}{r^5}, -\frac{(\beta y^2 + \beta x^2 - 2 \alpha r^2) C}{r^5} \right]$$


(%i6) alpha: Omega*r*cos(Omega*r) - sin(Omega*r);
(%o6)  $\Omega r \cos(\Omega r) - \sin(\Omega r)$ 

(%i7) %beta: 3*alpha+Omega^2*r^2*sin(Omega*r);
(%o7)  $\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r))$ 

(%i8) r: sqrt(x^2+y^2+z^2);
(%o8)  $\sqrt{z^2 + y^2 + x^2}$ 

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(%i9) W2: ev(W);
(%o9) [ -
```

$$\left( \frac{\Omega(\Omega r \cos(\Omega r) - \sin(\Omega r))y}{(z^2 + y^2 + x^2)^{3/2}} - \frac{(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))xz}{(z^2 + y^2 + x^2)^{5/2}} \right) C, -$$

$$\left( \frac{\Omega(\Omega r \cos(\Omega r) - \sin(\Omega r))x}{(z^2 + y^2 + x^2)^{3/2}} + \frac{(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))yz}{(z^2 + y^2 + x^2)^{5/2}} \right) C, -$$

$$\left( \frac{(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))(y^2 + x^2)}{(z^2 + y^2 + x^2)^{5/2}} - \frac{2(\Omega r \cos(\Omega r) - \sin(\Omega r))}{(z^2 + y^2 + x^2)^{3/2}} \right) C ]$$

## 2.2 Compute curl W

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(%i10) cW: curl(ev(W));
(%o10) [ ( -
```

$$\frac{3\Omega(\Omega r \cos(\Omega r) - \sin(\Omega r))xz}{(z^2 + y^2 + x^2)^{5/2}} +$$

$$\frac{(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))y}{(z^2 + y^2 + x^2)^{5/2}} -$$

$$\frac{5(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))yz^2}{(z^2 + y^2 + x^2)^{7/2}} ) C - ($$

$$\frac{2(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))y}{(z^2 + y^2 + x^2)^{5/2}} + \frac{6(\Omega r \cos(\Omega r) - \sin(\Omega r))y}{(z^2 + y^2 + x^2)^{5/2}} -$$

$$\frac{5(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))y(y^2 + x^2)}{(z^2 + y^2 + x^2)^{7/2}} ) C, ($$

$$\frac{2(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))x}{(z^2 + y^2 + x^2)^{5/2}} + \frac{6(\Omega r \cos(\Omega r) - \sin(\Omega r))x}{(z^2 + y^2 + x^2)^{5/2}} -$$

$$\frac{5(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))x(y^2 + x^2)}{(z^2 + y^2 + x^2)^{7/2}} ) C - ( -$$

$$\frac{3\Omega(\Omega r \cos(\Omega r) - \sin(\Omega r))yz}{(z^2 + y^2 + x^2)^{5/2}} - \frac{(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))x}{(z^2 + y^2 + x^2)^{5/2}} +$$

$$\frac{5(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))xz^2}{(z^2 + y^2 + x^2)^{7/2}} ) C, ( \frac{\Omega(\Omega r \cos(\Omega r) - \sin(\Omega r))}{(z^2 + y^2 + x^2)^{3/2}} -$$

$$\frac{3\Omega(\Omega r \cos(\Omega r) - \sin(\Omega r))y^2}{(z^2 + y^2 + x^2)^{5/2}} + \frac{5(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))xyz}{(z^2 + y^2 + x^2)^{7/2}} ) C -$$

$$( \frac{\Omega(\Omega r \cos(\Omega r) - \sin(\Omega r))}{(z^2 + y^2 + x^2)^{3/2}} - \frac{3\Omega(\Omega r \cos(\Omega r) - \sin(\Omega r))x^2}{(z^2 + y^2 + x^2)^{5/2}} -$$

$$\frac{5(\Omega^2 r^2 \sin(\Omega r) + 3(\Omega r \cos(\Omega r) - \sin(\Omega r)))xyz}{(z^2 + y^2 + x^2)^{7/2}} ) C ]$$

```

[ (%i11) kill(r,alpha,%beta);
[ (%o11) done

[ (%i12) cW1: ratsubst(r, sqrt(x^2+y^2+z^2), cW);
[ (%o12) [ - ( ((5 Ω^2 r^2 - 15) sin(Ω r) + 15 Ω r cos(Ω r)) y z^2 +
(3 Ω^2 r^3 cos(Ω r) - 3 Ω r^2 sin(Ω r)) x z +
((15 - 5 Ω^2 r^2) sin(Ω r) - 15 Ω r cos(Ω r)) y^3 + (
((15 - 5 Ω^2 r^2) sin(Ω r) - 15 Ω r cos(Ω r)) x^2 + (Ω^2 r^4 - 9 r^2) sin(Ω r) + 9 Ω r^3
cos(Ω r)) y) C) / r^7 , - ( ((5 Ω^2 r^2 - 15) sin(Ω r) + 15 Ω r cos(Ω r)) x z^2 +
(3 Ω r^2 sin(Ω r) - 3 Ω^2 r^3 cos(Ω r)) y z +
((5 Ω^2 r^2 - 15) sin(Ω r) + 15 Ω r cos(Ω r)) x y^2 +
((5 Ω^2 r^2 - 15) sin(Ω r) + 15 Ω r cos(Ω r)) x^3 +
((15 r^2 - 3 Ω^2 r^4) sin(Ω r) - 15 Ω r^3 cos(Ω r)) x) C) / r^7 , ( (
((10 Ω^2 r^2 - 30) sin(Ω r) + 30 Ω r cos(Ω r)) x y z +
(3 Ω r^2 sin(Ω r) - 3 Ω^2 r^3 cos(Ω r)) y^2 + (3 Ω^2 r^3 cos(Ω r) - 3 Ω r^2 sin(Ω r)) x^2)
C) / r^7 ]

[ (%i13) cW2: ratsubst(alpha, Omega*r*cos(Omega*r) - sin(Omega*r), cW1);
[ (%o13) [ - ( ((5 Ω^3 r^3 cos(Ω r) - 5 alpha Ω^2 r^2 + 15 alpha) y z^2 + 3 alpha Ω r^2 x
z + (-5 Ω^3 r^3 cos(Ω r) + 5 alpha Ω^2 r^2 - 15 alpha) y^3 + (
(-5 Ω^3 r^3 cos(Ω r) + 5 alpha Ω^2 r^2 - 15 alpha) x^2 + Ω^3 r^5 cos(Ω r) - alpha Ω^2 r^4 +
9 alpha r^2) y) C) / r^7 , - ( ((5 Ω^3 r^3 cos(Ω r) - 5 alpha Ω^2 r^2 + 15 alpha) x z^2 - 3
alpha Ω r^2 y z + (5 Ω^3 r^3 cos(Ω r) - 5 alpha Ω^2 r^2 + 15 alpha) x y^2 +
(5 Ω^3 r^3 cos(Ω r) - 5 alpha Ω^2 r^2 + 15 alpha) x^3 +
(-3 Ω^3 r^5 cos(Ω r) + 3 alpha Ω^2 r^4 - 15 alpha r^2) x) C) / r^7 ,
((10 Ω^3 r^3 cos(Ω r) - 10 alpha Ω^2 r^2 + 30 alpha) x y z - 3 alpha Ω r^2 y^2 + 3 alpha Ω r^2 x^2) C
r^7
]

```

## 2.3 Compute div W

```

[ (%i14) div(W);
[ (%o14) 0

```

## 2.4 Create plot data

```

[ (%i15) /*filebase: "D:/Doc/Artikel-Eck/ECE-Theorie/Paper258/"*/
filebase: "F:/Paper258/";
[ (%o15) F:/Paper258/

```

```

[ (%i16) filename: concat (filebase, "x1.dat");
  (%o16) F:/Paper258/x1.dat

[ (%i17) numer: true;
      stream: openw(filename);
      printf(stream, "# x1 x2 x3 v1 v2 v3 cv1 cv2 cv3~%");
  (%o17) true
  (%o18) Stream [STRING-CHAR]
  (%o19) false

[ (%i20) C: -1; Omega: 1;
  (%o20) -1
  (%o21) 1

[ (%i22) r: sqrt(x^2+y^2+z^2);
  (%o22) (z^2+y^2+x^2)^0.5

[ (%i23) alpha: Omega*r*cos(Omega*r) - sin(Omega*r);
  (%o23) (z^2+y^2+x^2)^0.5 cos((z^2+y^2+x^2)^0.5)-sin((z^2+y^2+x^2)^0.5)

[ (%i24) f: 1.$
      for k:-3.001 step 3 thru 3.001 do (
        nf: 0,
        z: k/2,
        for j:-4 step 1 thru 4 do (
          y: j/2,
          for i:-4 step 1 thru 4 do (
            x: i/2,
            x1: [x,y,z],
            v1: ev(ev(W2)),
            cv1: ev(ev(cW2))*f,
            /*print (x1,v1,cv1),*/
            w1: x1,
            w2: v1*f,
            w3: cv1*f,
            nf: nf+1,
            wa[nf]: append(w1, w2, w3)
          )
        ),
        for n:1 thru nf do write_data(wa[n], stream),
        printf(stream, "~%"),
        printf(stream, "~%")
      );
  (%o25) done

[ (%i26) close(stream);
  (%o26) true

```