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(%i1) kill(all);
(%o0) done

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1 Eqs.(24,25)

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(%i1) E22: dx = cos(theta)*dr-r*sin(theta)*dtheta;
(%o1) dx=dr cos(θ)-dtheta r sin(θ)

(%i2) E23: dy = sin(theta)*dr+r*cos(theta)*dtheta;
(%o2) dy=dr sin(θ)+dtheta r cos(θ)

(%i3) trigsimp(solve([E22,E23], [dr,dtheta]));
(%o3) [[dr=dy sin(θ)+dx cos(θ), dtheta=- $\frac{dx \sin(\theta)-dy \cos(\theta)}{r}$ ]]

```

2 Eq.(35)

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(%i4) depends(psi, theta);
(%o4) [Ψ(θ)]

(%i5) E35: -h[bar]^2/(2*m*rB^2)*diff(psi,theta,2) = (k/rB+E)*psi;
(%o5) 
$$-\frac{h_{\text{bar}}^2 \left(\frac{\text{d}^2}{\text{d} \theta^2} \Psi\right)}{2 m rB^2} = \Psi\left(\frac{k}{rB} + E\right)$$


(%i6) E: -m*k^2/(2*n^2*h[bar]^2);
(%o6) 
$$-\frac{k^2 m}{2 h_{\text{bar}}^2 n^2}$$


(%i7) E35a: ev(E35);
(%o7) 
$$-\frac{h_{\text{bar}}^2 \left(\frac{\text{d}^2}{\text{d} \theta^2} \Psi\right)}{2 m rB^2} = \Psi\left(\frac{k}{rB} - \frac{k^2 m}{2 h_{\text{bar}}^2 n^2}\right)$$


(%i8) E35b: solve(E35a, diff(psi,theta,2));
(%o8) [
$$\frac{\text{d}^2}{\text{d} \theta^2} \Psi = \frac{k^2 m^2 \Psi rB^2 - 2 h_{\text{bar}}^2 k m n^2 \Psi rB}{h_{\text{bar}}^4 n^2}$$
]

(%i9) E35c: expand(E35b);
(%o9) [
$$\frac{\text{d}^2}{\text{d} \theta^2} \Psi = \frac{k^2 m^2 \Psi rB^2}{h_{\text{bar}}^4 n^2} - \frac{2 k m \Psi rB}{h_{\text{bar}}^2}]$$


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✓ (%i10) rB: h[bar]/(m*c)*n^2/alpha[f];
      hbar n2
      ┌─────────┐
      │ c αf m
      └─────────┘

✓ (%i11) alpha[f]: k/(h[bar]^c);
      k
      ┌─────────┐
      hbar c

✓ (%i12) ev(ev(E35c));
      ┌─────────────────┐
      [ d2
      ─── Ψ = - n2 Ψ
      d θ2
```