

### 318(4) : A Theory of Counter Gravitation in E(1,2)

Consider the electromagnetic and gravitational potential equations of the previous note:

$$(\nabla^2 + \kappa_0^2) \phi = -\frac{\rho}{\epsilon_0} \quad - (1)$$

and

$$(\nabla^2 + \kappa_0^2) \Phi = -4\pi G \rho_m \quad - (2)$$

where

$$\kappa_0^2 = 2 \underline{\nabla} \cdot \underline{\omega} \quad - (3)$$

For simplicity assume that:

$$\rho = \frac{e_1}{V} \quad - (4)$$

and

$$\rho_m = \frac{M}{V} \quad - (5)$$

where  $V$  is a given sample volume. The total potential energy of the system is:

$$U = e\phi + m\Phi \quad - (6)$$

where:

$$(\nabla^2 + \kappa_0^2) U = -\frac{1}{V} \left( \frac{ee_1}{\epsilon_0} + 4\pi G_m M \right) \quad - (7)$$

2) The acceleration due to gravity is:

$$\underline{g} = -\frac{1}{m} (\underline{\nabla} \cdot \underline{U} + 2\underline{U} \underline{\omega}) \quad - (8)$$

In order to produce counter gravitation  $\underline{g}$   
must be made less negative, i.e. less attractive

Now define:

$$A \cos(\underline{k} \cdot \underline{r}) = -\frac{1}{\underline{\nabla}} \left( \frac{ee_1}{\epsilon_0} + 4\pi G \rho M \right) \quad - (9)$$

Here:

$$(\underline{\nabla}^2 + k_0^2) \underline{U} = A \cos(\underline{k} \cdot \underline{r}) \quad - (10)$$

which is an undamped Euler Bernoulli equation  
with solution:

$$\underline{U} = \frac{A \cos(\underline{k} \cdot \underline{r})}{k_0^2 - k^2} \quad - (11)$$

In the  $Z$  axis:

$$\underline{U} = \frac{A \cos k_z Z}{k_0^2 - k^2} \quad - (12)$$

From eqs (8) and (12), the acceleration

3) due to gravity in the  $z$ -axis is:

$$g_z = \frac{A}{m(k_0^2 - k^2)} \left( k_z \sin(k_z z) - \omega_z \cos(k_z z) \right) \quad - (13)$$

At the point:

$$k_z \sin(k_z z) = \omega_z \cos(k_z z) \quad - (14)$$

it follows that:

$$\boxed{g_z = 0} \quad - (15)$$

i.e. gravity has been reduced to zero:

$$\text{Using } \sin^2(k_z z) + \cos^2(k_z z) = 1 \quad - (16)$$

it follows from eqs. (14) and (16) that:

$$\cos(k_z z) = \left( 1 + \left( \frac{\omega_z}{k_z} \right)^2 \right)^{-1/2} \quad - (17)$$

$$\text{and } \sin(k_z z) = \left( 1 + \left( \frac{k_z}{\omega_z} \right)^2 \right)^{-1/2} \quad - (18)$$

For small  $k_z$ :

$$4) \quad \sin(k_z z) \sim k_z z - (19)$$

So eqs. (18) and (19) give:

$$k_z^2 z^2 \left( 1 + \left( \frac{k_z}{\omega_z} \right)^2 \right) = 1 - (20)$$

which can be solved numerically to give an estimate of  $k_z$  in terms of  $z$  and  $\omega_z$ . For small  $k_z$  eq. (20) is the condition for vanishing gravitation.

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