

```
(%i15) kill(all);
(%o0) done
```

```
(%i1) assume(v0>0, c>0, gamma>0);
(%o1) [v0>0, c>0, gamma>0]
```

## □ **1 Vacuum mass velocity**

```
(%i2) E22: gamma^2=1/(1-v0^2/c^2);
(%o2)  $gamma^2 = \frac{1}{1 - \frac{v0^2}{c^2}}$ 
```

```
(%i3) E22a: expand(solve(E22, v0^2));
(%o3) [ $v0^2 = c^2 - \frac{c^2}{gamma^2}$ ]
```

```
(%i4) E22b: sqrt(first(E22a));
(%o4)  $v0 = \sqrt{c^2 - \frac{c^2}{gamma^2}}$ 
```

```
(%i5) v0 = c*sqrt(1-1/gamma^2);
(%o5)  $v0 = c \sqrt{1 - \frac{1}{gamma^2}}$ 
```

```
(%i6) ratsimp(E22b^2-%^2);
(%o6) 0 = 0
```

```
(%i7) g: 2.00231930436182;
      gamma: g-1;
(%o7) 2.00231930436182
(%o8) 1.00231930436182
```

```
(%i9) c: 2.99792458e8;
(%o9) 2.99792458 108
```

```
(%i10) E22c: ev(E22b);
(%o10) v0 = 2.0382626563005663 107
```

```
(%i11) %/c;
(%o11) 3.3356409519815204 10-9 v0 = 0.067989123872508
```

```
(%i12) v[vac]: rhs(E22c);
(%o12) 2.0382626563005663 107
```

□ **2 Hubble constant and universal absorption coefficient**

```
(%i13) H: 7.2e6/3.0857e22;  
[ (%o13) 2.3333441358524806 10-16
```

```
(%i14) alpha[univ] = H/v[vac];  
[ (%o14)  $\alpha_{univ} = 1.1447710767990447 \cdot 10^{-23}$ 
```