

1) 177(4): Calculation of Force Eigenvalue of  $\psi_0$  H Atom

In  $\psi_0$  simplest case of  $\psi_0$  is radial wave function:

$$\psi_{10} = 2 \left( \frac{1}{a} \right)^{3/2} e^{-r/a} \quad - (1)$$

where  $a$  is the Bohr radius.  $\therefore A e^{-r/a}$  the relevant equation is:

$$(\hat{H} - E) \frac{d\psi_{10}}{dr} = F \psi_{10} \quad - (2)$$

The Hamiltonian is:

$$\hat{H} = \left( -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial r^2} + V \right) \quad - (3)$$

where 
$$V = -\frac{e^2}{4\pi\epsilon_0 r} + \frac{l(l+1)\hbar^2}{2m r^2} \quad - (4)$$

where  $l$  is the orbital angular momentum quantum number.  
For  $\psi_0$  is orbital:  $l = 0, \quad - (5)$

and the energy level is:

$$E = -\frac{\hbar^2}{2ma^2} \quad - (6)$$

Therefore:

$$\frac{d\psi_{10}}{dr} = -\frac{1}{a} \psi_{10} \quad - (7)$$

$$\frac{d^2\psi_{10}}{dr^2} = \frac{1}{a^2} \psi_{10} \quad - (8)$$

$$\frac{d^3\psi_{10}}{dr^3} = -\frac{1}{a^3} \psi_{10} \quad - (9)$$

Therefore:

$$2) \quad (\hat{H} - E) \frac{d\psi_{10}}{dr} = \left( \frac{L^2}{2ma^3} + \frac{e^2}{4\pi\epsilon_0 r a} - \frac{L^2}{2ma^3} \right) \psi_{10} \\ = F_{10} \psi_{10} \quad - (10)$$

So:

$$F_{10} = \frac{e^2}{4\pi\epsilon_0 r a} \quad - (11)$$

Conclusion

This is a pos.ive valued, pure quantum, force that counterbalances the classical force of attraction

$$F(\text{classical}) = -\frac{e^2}{4\pi\epsilon_0 r^2} \quad - (12)$$

from eq. (4)

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