

# Notes 56(3)

## Field Equations of a Class of Electromagnetic AB Effects

These effects are defined as follows. In regions where there are no fields present:

$$F = 0 \quad - (1)$$

$$D \wedge A = 0. \quad - (2)$$

In the absence of gravitation, eq. (2) means:

$$d \wedge A^1 = g A^2 \wedge A^3 \quad - (3)$$

$$d \wedge A^2 = g A^3 \wedge A^1 \quad - (4)$$

$$d \wedge A^3 = g A^1 \wedge A^2 \quad - (5)$$

$$d \wedge A^0 = - d \wedge A^3 = -g A^1 \wedge A^2. \quad - (6)$$

Eqs (3) to (6) define the electromagnetic AB potentials in regions where there are no fields.

In regions where there are fields present:

$$F = D \wedge A \neq 0 \quad - (7)$$

and

$$F^1 = d \wedge A^1 - g A^2 \wedge A^3 \quad - (8)$$

$$F^2 = d \wedge A^2 - g A^3 \wedge A^1 \quad - (9)$$

$$F^3 = d \wedge A^3 - g A^1 \wedge A^2. \quad - (10)$$

## Standard Model

In the standard model there is no explanation for the AB effects because:

$$F = dA \quad - (11)$$

So if  $A$  is zero  $F$  is zero and if  $F$  is zero  $A$  is zero. A potential cannot exist in the absence of a field in the standard model.

## Gauge Theory

The usual attempts to rectify this anomaly in the standard model are based on a gauge transformation:

$$A \rightarrow A + dx \quad - (12)$$

and the Poincaré Lemma:

$$d \wedge dx = 0. \quad - (13)$$

The Stokes Theorem is then used to claim

that 
$$\int_S d \wedge dx \neq 0 \text{ (?) } - (14)$$

As shown in Vol. 1 of "Generally Covariant Unified Field Theory" (Abrams 2005), this claim is mathematically correct.

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4) The generally covariant Stokes theorem must be used in FCF theory (vol 1 and pages 29 of vol 2):

$$\int_S F = \oint A \quad - (15)$$

Therefore if  $F = 0$ ,

$$\int_S D \wedge A = 0 \quad - (16)$$

i.e.

$$\int_S d \wedge A^1 = \int_S g A^2 \wedge A^3 \neq 0 \quad - (17)$$

$$\int_S d \wedge A^2 = \int_S g A^3 \wedge A^1 \neq 0 \quad - (18)$$

$$\int_S d \wedge A^3 = - \int_S d \wedge A^3 = - \int_S g A^1 \wedge A^2 \neq 0 \quad - (19)$$

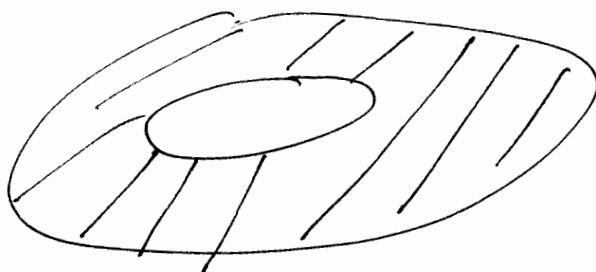
The Chern-Simons effect is due to surface integrals such as those in eqs. (17) to (19). The area is defined by the paths of the electron beams as is well known.

5) Inside the <sup>shaded</sup> area of Fig (1):

$$\int_S F = 0 \quad - (20)$$

AB experiments can be understood by defining an area inside another:

Fig (1)



The surface integral in eq. (20) refers to the shaded area in Fig (1) and excludes the inner area, representing the inner whisker and  $F \neq 0$  in the Chambers experiment. The surface integral in eqs. (17) to (19) also refers to the shaded area in Fig (1), i.e. the area where  $F = 0$ . In this area the surface integrals in eqs. (17) to (19) are not-zero.

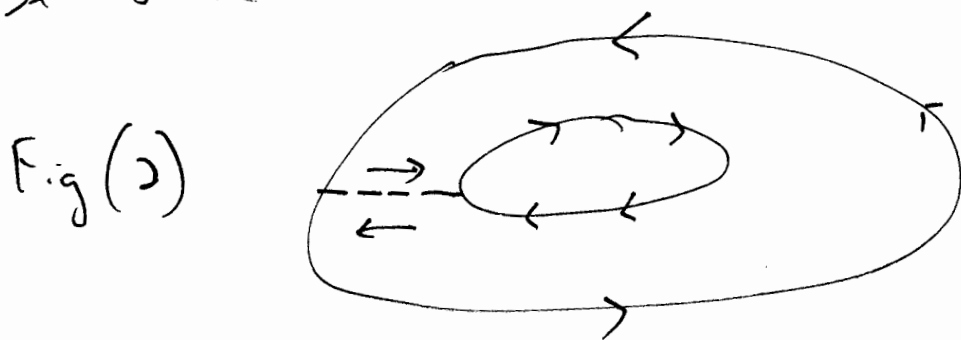
In the standard model, the AB effect is incorrectly attributed to:

$$\int_S d n d\phi \neq 0 \quad (?) \quad - (21)$$

) is the shaded area of Fig (1). This is incorrect because by Stokes' theorem:

$$\int_S d\Lambda dx = 0 \quad - (22)$$

for all  $\chi$ . The correct contour integral to be used is:



and produces the result that there is NO AB effect

$$\int_S d\Lambda dx = \oint dx = 0 \quad - (23)$$

for ANY function  $\chi$ .

This serious error in the standard model has been accepted unthinkingly for years. The correct explanation of any AB effect always requires a generally covariant unified field theory (i.e. ECE theory).

8) The Aharonov-Bohm effect is observed experimentally to be the integral over the magnetic flux density of  $\vec{B}$  in which over the area of total area enclosed in Fig (1). In the shaded area there is no magnetic flux density, but there is a non-zero potential  $A_1$ .

So the Aharonov-Bohm effect is :

$$\int_S \vec{F} = \int_S \nabla \wedge A = \oint A \quad - (24)$$

w.r.t :

$$\int_S \nabla \wedge A_1 (\text{shaded area}) = 0, \quad - (25)$$

$$\int_S \nabla \wedge A (\text{inner area}) \neq 0. \quad - (26)$$

The  $A_1$  in the shaded area is different from the  $A$  in the inner area. The effect is due to the  $A_1$  of the shaded area causing momentum to a free electron via eq. (11).