

q4(2): Second Resonance Equation for the Bedouin Motor

The source of this second resonance equation is:

$$\underline{\nabla} \times \frac{\partial \underline{A}}{\partial t} - \frac{\partial \underline{\omega}}{\partial t} \times \underline{A} - \underline{\omega} \times \frac{\partial \underline{A}}{\partial t} = \left(\frac{\partial \underline{B}}{\partial t} \right)_{\text{driving term}} \quad (1)$$

Now differentiate eq. (1) with respect to t :

$$\frac{\partial^2}{\partial t^2} (\underline{\nabla} \times \underline{A}) + \frac{\partial}{\partial t} (\underline{A} \times \frac{\partial \underline{\omega}}{\partial t}) + \frac{\partial}{\partial t} \left(\frac{\partial \underline{A}}{\partial t} \times \underline{\omega} \right) = \left(\frac{\partial^2 \underline{B}}{\partial t^2} \right)_{\text{driving term}}$$

i.e.:

$$\underline{\nabla} \times \frac{\partial^2 \underline{A}}{\partial t^2} + \frac{\partial \underline{A}}{\partial t} \times \frac{\partial \underline{\omega}}{\partial t} + \underline{A} \times \frac{\partial^2 \underline{\omega}}{\partial t^2} = \left(\frac{\partial^2 \underline{B}}{\partial t^2} \right)$$

$$+ \frac{\partial^2 \underline{A}}{\partial t^2} \times \underline{\omega} + \frac{\partial \underline{A}}{\partial t} \times \frac{\partial \underline{\omega}}{\partial t}$$

$$\left(\underline{\nabla} \times \frac{\partial^2 \underline{A}}{\partial t^2} + \frac{\partial^2 \underline{A}}{\partial t^2} \times \underline{\omega} \right) + 2 \frac{\partial \underline{A}}{\partial t} \times \frac{\partial \underline{\omega}}{\partial t} + \underline{A} \times \frac{\partial^2 \underline{\omega}}{\partial t^2} = \left(\frac{\partial^2 \underline{B}}{\partial t^2} \right)_{\text{driving term}} \quad (2)$$

This is a resonance equation in \underline{A} , given $\underline{\omega}$, and for $\underline{\omega}$, given \underline{A} . Models and simplifications of eq. (2) could be used, or resonance solutions sought by computer.